FACULTY OF INFORMATICS
M.C.A. (2 Years Course) I- Semester (CBCS) (Main \& Backlog) Examination, April/May 2023

## Subject: Probability and Statistics

## Time: 3 Hours

Max. Marks: 70
Note: I. Answer one question from each unit. All questions carry equal marks. II. Missing data, if any, may be suitably assumed.

## Unit-I

1. a) Explain about Vector Spaces and Subspaces.
b) Prove the set of solutions ( $x, y, z$ ) of the equations $x+y+2 z=0$ is a subspace of the space $R^{3}(R)$.
2. a) Define column space of a $(m \times n)$ matrix $A$.
b) Determine Whether set of polynomial form a basis of $\mathrm{P}_{3}$.

$$
5-3 \mathrm{t}+4 \mathrm{t}^{2}+2 \mathrm{t}^{3},
$$

$9+t+8 t^{2}-6 t^{3}$, $6-2 t+5 t^{2}$, $\mathrm{t}^{3}$.

## Unit - II

3. a) Explain types of Events.
b) State and prove Baye's theorem.
4.a) What is Random Variable.
b) Three cards are drawn at random successively with replacements from a well shuffled pack of cards. Getting a card of diamond is termed as a success. Obtain the probability distribution of the number of success.

## Unit - III

5. a) What is Random Sampling?
b)The heights of 10 males of a given locality are found to be $70,67,62,68,61,68,70,64,64$ and 66 inches. Is it reasonable to believe that the average height is greater than 64 inches.(Table value $=1.833$ )
6. a) Define Interval Estimates.
b) Explain Random and Non Random sampling.

Unit - IV
7. a) What is standard deviation?
b) A Random sample of 40 student selected from a college and their average height is found to be 175 cms with a standard deviation of 10 cms .Another sample of 50 students selected from a college, their average height is found to be 170 cms . with a standard deviation of 4 cms . Test an average, the average height of the students of $1^{\text {st }}$ college is $>2^{\text {nd }}$ college.
(OR)
8. a) Explain large sample test.
b) Before increasing the exercise duty 40 out of 70 were smokers, after increasing the tax a random sample of 150 persons selected. In this sample 90 persons were found smokers. Test, is there any decrease in the proportion of smokers after increasing the tax.

## Unit - V

9. a) Define (i)
(i) Population
(ii) Sample
(iii) Parameter
(iv) Statistics
(v) Standard error
b) A survey of 320 families with 5 children each revealed the following distribution:

No. of boys: $\begin{array}{lllllll}5 & 4 & 3 & 2 & 1 & 0\end{array}$
No. of girls: $\begin{array}{lllllll}0 & 1 & 2 & 3 & 4 & 5\end{array}$
No. of Families: $\begin{array}{lllllll}14 & 56 & 110 & 68 & 40 & 12\end{array}$
Is this result consistent with the hypothesis that male and female births are equally probable.
(OR)
10. a) The following are the regression lines $8 x-10 y+66=0$ and $40 x-18 y=214$. Find:
i) Regression equation $Y$ on $X$.
ii) Correlation coefficient between $X$ and $Y$
b) The following are the regression lines $8 x-10 y+66=0$ and $40 x-18 y=214$.Find:
i) Regression equation $X$ on $Y$.
ii) Mean Values of $X$ and $Y$

